## Video Signals

Date: 22 January 2024
Ex.1.[8 pts] In the plot below it is represented the Hough transform of a set of points. What are their position in the 2D Cartesian plane? (Justify the answer).


Ex.2.[8 pts] The following values represent the intensities of an image portion. For the central part (inside the thicker border) evaluate the Local Binary Pattern.

| 70 | 177 | 112 | 47 |
| :---: | :---: | :---: | :---: |
| 11 | 81 | 97 | 125 |
| 24 | 243 | 195 | 114 |
| 210 | 8 | 203 | 165 |

## Ex.3.[6 pts]



Consider the $\mathrm{B} / \mathrm{W}$ object on the left, describe the morphological procedure to extract its edge.
Describe the whole procedure using this structuring element.


Furthermore, define a stopping condition for the algorithm.

## Es.3. [11 pts to be solved writing on the paper a suitable MATLAB code]

You have to implement a medical application able to extract the vessels from a retina image, like the one shown below.


Write a MATLAB script able to perform the following steps:
a) Read the 'eye.jpg' image, convert it to a double representation and visualize it.
b) Convert the image to grayscale and apply a $7 \times 7$ gaussian filter with sigma equal to 0.5 , obtaining image $B$.
c) Using a $5 \times 5$ square structuring element apply a dilation to $B$, obtaining $C$.
d) Obtain $D$ by calculating the pixelwise ratio between $B$ and $C$ (hint: add a small quantity to avoid dividing by 0 ).
e) Using Sobel kernels calculate the gradient magnitude of B. Apply a morphological dilation with the same structuring element used in c) to obtain $E$.
f) Define thr_1 and thr_2 as the average values of $D$ and $E$ respectively. Obtain $F$ by setting to true all the pixels in which $D$ is less than thr_1 and $E$ is greater than $t h r_{-} 2$.
g) Assign a label to all the connected components of F .
h) Initialize a mask called H to zeroes and, going through all the connected components, find the ones having a pixel area (count the pixels) greater than 50 . For these ones set the corresponding pixels of H to one.
i) Apply the mask H to the input color image by setting all the pixels

## List of possible Matlab functions

figure
im2double
imread
rgb2gray
imcrop
imfilter
imhist
imopen rgb2ind
histeq
hist
imshow
fspecial
imerase
strel
imdilate bwlabel having false value in H to black and visualize the result.

## Solutions

## Es. 1

Considering the equation $\rho=x \cos (\vartheta)+y \sin (\vartheta)$ for each curve, we can assert that all of them pass through the point $\rho=2, \quad \vartheta=0, \quad \rightarrow 2=x \cdot 1+y \cdot 0 \rightarrow x=2$
Then we can set three further equations:
$3=x \cos \left(\frac{\pi}{2}\right)+y \sin \left(\frac{\pi}{2}\right) \rightarrow y=3$
$0=x \cos \left(\frac{\pi}{2}\right)+y \sin \left(\frac{\pi}{2}\right) \rightarrow y=0$
$-3=x \cos \left(\frac{\pi}{2}\right)+y \sin \left(\frac{\pi}{2}\right) \rightarrow y=-3$
The points will be $P_{1}(2,-3), P_{2}(2,0), P_{3}(2,3)$

## Es. 2

According to the Local Binary Pattern approach, starting from the North (Pixel above the considered one) and moving in a clockwise direction, we get the following walues:
$\left[\begin{array}{ll}11111000 & 10111101 \\ 00000000 & 00001010\end{array}\right] \rightarrow\left[\begin{array}{cc}248 & 189 \\ 0 & 5\end{array}\right]$

## Es. 3

Details on morphological edge extraction can be found in lectures.
The result will be:


## Es. 4

```
clc
close all
clear all
%a)
img = im2double(imread('eye.jpg'));
figure
imshow(img)
%b) convert to gray
gray = rgb2gray(img);
g = fspecial('gaussian',7,0.5);
B = imfilter(gray,g,'conv','sym','same');
%C)
s = strel('square',5);
C = imdilate(B,s);
%d)
D = B./(C+0.001);
%e)
k = fspecial('sobel');
i_x = imfilter(B,k,'conv','sym','same');
i_Y = imfilter(B,k','conv','sym','same');
grad = sqrt(i_x.^2 + i_y.^2);
E = imdilate(grad,s);
%f)
thr_1 = mean(D(:));
thr_2 = mean(E(:));
F = D<thr_1 & E>thr_2;
%g)
label = bwlabel(F);
%h)
H = zeros(size(label));
thr = 50;
for i = 1:max(label(:))
    mask_loc = (label == i);
    area_= sum(mask_loc(:));
    if(area>thr)
        H = H+mask_loc;
    end
end
%i)
output = H.*img;
figure
imshow(output)
```

