

Multimedia Signal Processing 1st Module
Fundamentals of Multimedia Signal Processing

19/2/2018

Ex.1 (Pt.14)

We want to process a signal sampled at 10kHz using a digital band-stop filter able to:

Completely remove the component at 2.5kHz

Preserve with the original amplitude the components at 0kHz and at 5kHz.

In order to design and analyze such a filter,

1. Provide the filter $H[k]$ of 4 samples in the frequency domain satisfying the aforementioned constraints [2pts]
2. Define the Inverse Discrete Fourier Transform Matrix for the filter and calculate time-domain version $h[n]$ of it [5pts]
3. Find the attenuation of the filter for a sinusoid at 1.25kHz [3Pts].
4. Filter the following signal $x[n]$ working in the time domain using the Overlap and Add approach [4 Pts].

$$x[n]=\{1,-1,-3,-1,1,-1,-3,-1, 1\}$$

Ex.2 (Pt.9)

A signal is made of two sinusoids at 100kHz and 150kHz. The signal is sampled at 900kHz. Which is the minimum length of a Bartlett window in order to make the two signals completely distinguishable?

Window Type	Peak Sidelobe Amplitude (Relative, dB)	Approximate Width of Main Lobe	Peak Approximation Error, $20\log(\delta)$ (dB)
Rectangular	-13	$\frac{4\pi}{M+1}$	-21
Bartlett	-25	$\frac{8\pi}{M}$	-25
Hann	-31	$\frac{8\pi}{M}$	-44
Hamming	-41	$\frac{8\pi}{M}$	-53
Blackman	-57	$\frac{12\pi}{M}$	-74

Ex.3 (Pt. 11 – MATLAB code)

1. [7 pts] Write a MATLAB function

```
[z, p, b, a]=all_pass(z,p,b,a)
```

that receives as input one among the zeros, the poles, the numerator or the denominator of the difference equations of a filter $H(z)$, and it returns the missing elements to build an all-pass filter.

Hint: look at the following point to see the use of the function

2. [4 pts] use the function to compute

```
[z,p,b,a]=all_pass([],[],b,[]);
```

with $b=[1,-0.8,0.6]$ and plot the transfer function in $N=512$ points.

Solutions

Ex.1

$$H[k]=\{1,0,1,0\}$$

$$W^{-1} = \frac{1}{4} \begin{bmatrix} 1 & 1 & 1 & 1 \\ 1 & j & -1 & -j \\ 1 & -1 & 1 & -1 \\ 1 & -j & -1 & j \end{bmatrix}$$

$$h[n]=W^{-1}H[k]=\{.5,0,.5,0\}$$

$$H(z) = \frac{1}{2} + \frac{1}{2}z^{-2} \rightarrow H\left(\omega = 2\pi \frac{1.25\text{kHz}}{10\text{kHz}} = \frac{\pi}{4}\right) = \frac{1}{2} + \frac{1}{2}e^{-j\frac{\pi}{2}} = \frac{1}{2} - \frac{1}{2}j$$

$$\left|H\left(\omega = \frac{\pi}{4}\right)\right| = \frac{\sqrt{2}}{2}$$

$$y[n]=h[n]*x[n]=\{0.5,-0.5,-1,-1,-1,-1,-1,-1,-1,-1\}$$

Ex.2

The two signals are represented in the Frequency domain as two impulses at the normalized frequencies

$$\omega_1 = \frac{100}{900}2\pi = \frac{2}{9}\pi$$

$$\omega_2 = \frac{150}{900}2\pi = \frac{1}{3}\pi$$

$$\Delta\omega = \frac{\pi}{9}$$

The minimum length of the Bartlett window will be:

$$\frac{8\pi}{M} = \frac{\pi}{9} \rightarrow M = 72$$

Ex.3

File: all_pass.m

```
function [z, p, b, a]=all_pass(z,p,b,a)
compute_ab=0;compute_zp=0;
if length(z)>0
p=1./conj(z);compute_ab=1;
elseif length(p)>0
z=1./conj(p);compute_ab=1;
elseif length(b)>0
a=fliplr(b);compute_zp=1;
elseif length(a)>0
b=fliplr(a);compute_zp=1;
end
if compute_ab==1
```

```
        a=poly(p);b=poly(z);
elseif compute_zp==1
        p=roots(a); z=roots(b);
end
end
```

File: script.m

```
b=[1,-0.8,0.6];
[z,p,b,a]=all_pass([],[],b,[]);

N=512;[H,w]=freqz(b,a,N);

figure;
subplot(2,1,1);plot(w,abs(H));
xlabel('\omega');ylabel('|H(z)|')
title('Magnitude');

subplot(2,1,2);plot(w,angle(H));
xlabel('\omega');ylabel('angle H(z)')
title('Phase');
```