

Multimedia Signal Processing 1st Module

Pre-examination
23 November 2009

Ex.1 (Pt.5)

Consider the filter $H(z)$ whose Transfer Function is: $H(z) = \frac{1 + 0.81z^{-2}}{1 + 0.49z^{-2}}$.

1. Define its block scheme in terms of inputs ($x(n)$) and outputs ($y(n)$).
2. Provide its zeros-poles diagram and draw an approximate behavior of its amplitude and phase response at different normalized frequencies.
3. If the filter is a “minimum phase” transform it into a “maximum phase” or vice-versa preserving the same amplitude response. Provide a new phase diagram accordingly to the modifications.

Ex.2 (Pt.5)

Consider a filter whose impulse response is

$$h(n) = \delta(n) - \delta(n-1) + 2\delta(n-2) - 2\delta(n-3) + 3\delta(n-4) - 3\delta(n-5).$$

1. Provide a polyphase implementation of its decimation of order 3 ($M=3$) and the associated structure (block diagram).
2. Using a decimation of order 2 ($M=2$) define a perfect reconstruction filter bank ($H_0(z)$, $H_1(z)$, $G_0(z)$, $G_1(z)$).

Ex.3 (Pt.5)

A Random Variable X has a Uniform Probability Density Function (pdf) between $\theta - \frac{1}{2}$ and $\theta + \frac{1}{2}$ (i.e. $\text{rect}(x - \theta)$). Three realizations of X are $x_1=1.5$, $x_2=1.7$, $x_3=2.5$.

1. Represent and quote the likelihood function $L(\theta | x_1, x_2, x_3)$.
2. How would change L if the 3 samples would be $x_1=1.6$, $x_2=1.7$, $x_3=2.4$? Provide a quoted representation

Ex.4 (Pt.5)

An autoregressive model for parametric spectral estimation of a random process provide us with a one pole filter ($a_1=-0.5$) for a white noise of power $\sigma^2=4$.

1. Find the autocovariance values $r(0)$, $r(1)$ and $r(2)$ of the final model.

Ex.5 (Pt.5)

Load the waveform ‘mtlb’ and determine the sampling frequency F_s .

Consider a LTI digital filter characterized by the following difference equation:

$$h(n) = -0.9 y(n-1) + x(n) + x(n-1)$$

Filter the input sequence $x(n)$ with $h(n)$ computing the convolution by means the OLA approach:

segment the signal $x(n)$ into overlapping frames of length 20ms using a Hamming window at 50% overlap.

Ex.6 (Pt.5)

Load the waveform ‘mtlb’ and determine the sampling frequency F_s .

Decimate the signal to the sampling frequency: $F = (p/q)F_s$ [$p=4$ and $q=5$].

Design the appropriate low-pass filters using the Matlab’s function ‘fir1’.